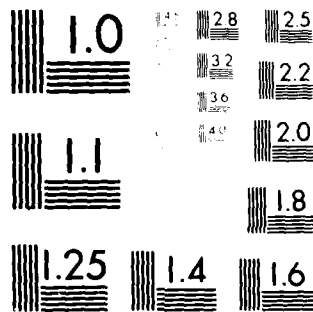


AD-A098 332 NAVAL RESEARCH LAB WASHINGTON DC F/G 20/9  
ON THE SPATIAL POWER SPECTRUM OF THE E X B GRADIENT DRIFT INSTA--ETC(U)  
APR 81 M J KESKINEN, S L OSSAKOW  
UNCLASSIFIED NRL-MK-4494 NL

1 x 1  
42 A  
048 550



END  
DATE  
FILMED  
5-81  
DTIC



MICROCOPY RESOLUTION TEST CHART  
NATIONAL BUREAU OF STANDARDS-1963-A

AD A098332

**P**  
ADM-AM-

NRL Memorandum Report 4494

⑥  
**On the Spatial Power Spectrum of the  
 $E \times B$  Gradient Drift Instability in  
Ionospheric Plasma Clouds.**

⑦ M. J. KERNEN S. L. OMAKOW

Geophysical and Plasma Dynamics Branch  
Plasma Physics Division

⑪ 14 Apr 81

12/24

⑨ April 14, 1981  
Memorandum rept.

This research was sponsored by the Defense Nuclear Agency under Subtask 599QAXHC,  
work unit 00002, and work unit title, "Plasma Structure Evolution"

⑫

⑬ 0000



NAVAL RESEARCH LABORATORY  
Washington, D.C.

254950

Approved for public release; distribution unlimited.

DTIC  
ELECTE  
S APR 30 1981 D

81 4 30 033

⑭

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM	
1. REPORT NUMBER NRL Memorandum Report 4494	2. GOVT ACCESSION NO. AD-A098	3. REPORT'S CATALOG NUMBER 332	
4. TITLE (and Subtitle) ON THE SPATIAL POWER SPECTRUM OF THE E X B GRADIENT DRIFT INSTABILITY IN IONOSPHERIC PLASMA CLOUDS		5. TYPE OF REPORT & PERIOD COVERED Interim report on a continuing NRL problem.	
		6. PERFORMING ORG. REPORT NUMBER	
7. AUTHOR(s) M. J. Keskinen and S. L. Ossakow		8. CONTRACT OR GRANT NUMBER(s)	
9. PERFORMING ORGANIZATION NAME AND ADDRESS Naval Research Laboratory Washington, DC 20375		10. PROGRAM ELEMENT PROJECT TASK AREA & WORK UNIT NUMBERS 47-0889-0-1	
11. CONTROLLING OFFICE NAME AND ADDRESS Defense Nuclear Agency Washington, DC 20305		12. REPORT DATE April 14, 1981	
		13. NUMBER OF PAGES 24	
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)		15. SECURITY CLASS (of this report) UNCLASSIFIED	
		15a. DECLASSIFICATION DOWNGRADING SCHEDULE	
16. DISTRIBUTION STATEMENT (of this Report)  Approved for public release; distribution unlimited.		Accession For NTIS GRA&I <input checked="" type="checkbox"/> DTIC TAB <input type="checkbox"/> Unannounced <input type="checkbox"/> Justification	
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		By Distribution/ Availability Dist	
18. SUPPLEMENTARY NOTES This research was sponsored by the Defense Nuclear Agency under Subtask S99QAXHC, work unit 00002, and work unit title, "Plasma Structure Evolution."		A	
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) E X B Gradient drift instability      Conservation laws Ionospheric plasma clouds Power spectrum Analytic formulation			
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) It is shown that the two dimensional power law spatial power spectra of magnetic field line integrated Pedersen conductivity perturbations in the plane perpendicular to the magnetic field recently computed from numerical simulation studies of ionospheric plasma clouds are consistent with conservation laws implied by the fundamental plasma fluid equations describing the E X B gradient drift instability in these ionospheric plasma clouds.			

DD FORM 1473  
1 JAN 73

EDITION OF 1 NOV 65 IS OBSOLETE  
S/N 0102-014-6601

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

## ON THE SPATIAL POWER SPECTRUM OF THE $\underline{E} \times \underline{B}$ GRADIENT DRIFT INSTABILITY IN IONOSPHERIC PLASMA CLOUDS

Experimental studies of plasma clouds in the ionosphere [Rosenberg, 1971; Davis et al., 1974; Baker and Ulwick, 1978] have yielded much data describing ambient ionospheric conditions, e.g., electric and magnetic fields. The characteristic initial steepening, elongation, and striation of  $\underline{E} \times \underline{B}$  drifting plasma clouds have been studied by applying the linear theory of the  $\underline{E} \times \underline{B}$  gradient drift instability, originally developed for laboratory gas discharges [Simon, 1963] to plasma cloud geometries [Haerendel et al., 1967; Linson and Workman, 1970; Völk and Haerendel, 1971; Perkins et al., 1973]. More recently Chaturvedi and Ossakow [1979] has presented arguments based on the nonlinear two-dimensional coherent mode coupling of two Fourier modes of plasma cloud density, following the work of Rognlien and Weinstock [1975], to explain the nonlinear stabilization and resultant saturated amplitudes and power spectra of the long wavelength  $\underline{E} \times \underline{B}$  gradient drift instability in ionospheric plasma clouds.

Numerical simulations [Zabusky et al., 1973; Lloyd and Haerendel, 1973; Goldman et al., 1974; Doles et al., 1976; Ossakow et al., 1975, 1977] of the interaction of barium plasma clouds with the ionosphere have reproduced not only many of the gross observational features of plasma cloud evolution, but also their spatial power spectra [Scannapieco et al., 1976], minimum striation scale sizes [McDonald et al., 1978, 1980] and outer scale size or correlation length [Keskinen et al., 1980a; Keskinen and Ossakow, 1980]. In addition numerical

Manuscript submitted February 3, 1981.

simulation studies of the  $\underline{E} \times \underline{B}$  gradient drift instability in local unstable regions of ionospheric plasma clouds [Keskinen et al., 1980b] have yielded spatial power spectra and saturated wave amplitudes consistent with experimental values.

However, to date, an analytical description of the two-dimensional spatial power spectra of the  $\underline{E} \times \underline{B}$  gradient drift instability in ionospheric plasma clouds over a wide range of wavelengths has not been discussed in detail. In this paper we show that the spatial power spectra of ionospheric plasma clouds recently computed from numerical simulation studies and experimental observations are consistent with conservation laws implied by the fundamental fluid equations modeling the  $\underline{E} \times \underline{B}$  gradient drift instability in ionospheric plasma clouds.

For wavelengths much greater than the ion gyroradius (approximately 10 meters for  $Ba^+$  ions in the twilight F region), the dynamics of the plasma cloud and background ionosphere can be studied in the fluid approximation [Völk and Haerendel, 1971; Perkins et al., 1973; Zabusky et al., 1973; Ossakow et al., 1975]. For large clouds (large magnetic field line integrated Pedersen conductivity compared with that of the background ionosphere), the cloud interaction with the background ionosphere (second level) can be neglected [Haerendel et al., 1967]. Furthermore, due to the very high conductivity along the magnetic field lines (typically  $\sigma_p / \sigma_{||} \approx 10^{-6}$  with  $\sigma_p$  and  $\sigma_{||}$  the Pedersen and parallel conductivities respectively) the field lines may be regarded as equipotentials and, as a result, a

field line integrated (two-dimensional) model is justified [Volk and Haerendel, 1971; Perkins et al., 1973]. In reality, an artificially injected plasma cloud will, initially, be two-dimensional in the plane perpendicular to the magnetic field. But a two-dimensional plasma cloud of finite extent is not stationary [Dungey, 1958] and will distort as it convects. However, for striation scale sizes less than the ambient cloud Pedersen conductivity gradient scale length and on the faster time scale on which striations develop, the assumption of one-dimensionality is justified. As a result, in what follows we confine our attention to local regions of initially slablike (one-dimensional) ionospheric plasma clouds. This will also facilitate comparison with numerical simulation studies.

By adopting a Cartesian coordinate system  $(x, y, z)$  with magnetic field  $B\hat{z}$ , ambient electric field  $E_0\hat{y}$ , and after transforming to a frame drifting with velocity  $\underline{V}_0 = (cE_0/B)\hat{x}$ , the two-dimensional model equations for the magnetic field line integrated plasma cloud Pedersen conductivity  $\Sigma(x, y)$  and the self-consistent plasma cloud electrostatic potential  $\delta\psi(x, y)$  can be written

$$\frac{\partial \Sigma}{\partial t} + \frac{c}{B} \hat{z} \times \nabla \delta\psi \cdot \nabla \Sigma = D \nabla^2 \Sigma \quad (1)$$

$$\nabla \cdot (\Sigma \nabla \delta\psi) = \underline{E}_0 \cdot \nabla \Sigma \quad (2)$$

where  $\nabla \delta\psi = -\underline{E}(x, y) + \underline{E}_0$ ,  $\underline{E}(x, y)$  the total electrostatic field,  $c$  is the speed of light,  $\nabla \equiv (\partial/\partial x, \partial/\partial y)$  and  $D$  is the cross-field diffusion coefficient [Perkins et al., 1973] given by  $2(v_e/\Omega_e)(ck_B T/eB)$  with  $T$  the ion and electron temperature,

$\nu_e$  the sum of electron collision frequencies with plasma cloud ions and ambient neutrals,  $k_B$  is Boltzmann's constant, and  $\Omega_e$  the electron gyrofrequency. All other symbols retain their conventional meaning. Equation (1) results from the magnetic field line integration (along the z-direction) of the ion continuity equation, while equation (2) is derived from current conservation  $\nabla \cdot \underline{J} = 0$ .

By linearizing (1) and (2) and assuming fluctuations in magnetic field line integrated-Pedersen conductivity and cloud potential  $\delta\Sigma, \delta\varphi \propto \exp \left[ i(k_y y + k_x x) + \gamma_{\underline{k}} t \right]$  with  $\underline{k} \cdot \underline{B} = 0$ ,  $kL \gg 1$ , one finds the usual  $\underline{E} \times \underline{B}$  growth rate

$$\gamma_{\underline{k}} = (cE_0/BL)(k_y/k)^2 - Dk^2 \quad (3)$$

where  $k^2 = k_x^2 + k_y^2$ ,  $L^{-1} = \partial \ln \Sigma_0 / \partial x$ . For  $cE_0/B = 100$  m/sec,  $L = 6$  km,  $D = 1 \text{ m}^2/\text{sec}$ , the critical wavelength  $\lambda_c$  ( $\gamma_{\underline{k}} = 0$ )  $\approx 60$  m.

We will now show that several features of the spatial power spectra of the  $\underline{E} \times \underline{B}$  gradient drift instability in ionospheric plasma clouds as observed in experiments and recent numerical simulations can be derived by considering the conservation laws implied by (1) and (2). We can write (1) and (2), after making the separation  $\Sigma(x,y) = \Sigma_0(x) + \delta\Sigma(x,y)$ , as follows:

$$\frac{\partial \delta\Sigma}{\partial t} + \frac{c}{B} \hat{z} \times \nabla \delta\varphi \cdot \nabla \Sigma_0 + \frac{c}{B} \hat{z} \times \nabla \delta\varphi \cdot \nabla \delta\Sigma = D \nabla^2 \delta\Sigma \quad (4)$$

$$\Sigma_0 \nabla^2 \delta\varphi + \delta\Sigma \nabla^2 \delta\varphi + \nabla \Sigma_0 \cdot \nabla \delta\varphi + \nabla \delta\Sigma \cdot \nabla \delta\varphi = \underline{E}_0 \cdot \nabla \delta\Sigma \quad (5)$$

We first multiply (4) by  $\delta\Sigma$  and integrate over all  $x$  and  $y$  finding



$$\begin{aligned} \frac{1}{2} \frac{\partial}{\partial t} \int d^2x (\delta\Sigma)^2 + \frac{c}{B} \int d^2x \delta\Sigma \hat{z} \times \nabla \delta\psi \cdot \nabla \Sigma_0 \\ + \frac{c}{B} \int d^2x \delta\Sigma \hat{z} \times \nabla \delta\psi \cdot \nabla \delta\Sigma - D \int d^2x \delta\Sigma \nabla^2 \delta\Sigma = 0 \quad (6) \end{aligned}$$

where  $d^2x \equiv dx dy$ . The third term on the left hand side vanishes since

$$\begin{aligned} & \int d^2x \delta\Sigma \hat{z} \times \nabla \delta\psi \cdot \nabla \delta\Sigma \\ &= \frac{1}{2} \int d^2x \hat{z} \times \nabla \delta\psi \cdot \nabla (\delta\Sigma)^2 \\ &= \frac{1}{2} \int d^2x \nabla \cdot [(\delta\Sigma)^2 \hat{z} \times \nabla \delta\psi] \end{aligned}$$

$$= 0 \text{ if } (\delta\Sigma)^2 \rightarrow 0 \text{ as } x, y \rightarrow \infty.$$

since  $\nabla \cdot [(\delta\Sigma)^2 \hat{z} \times \nabla \delta\psi] = \hat{z} \times \nabla \delta\psi \cdot \nabla (\delta\Sigma)^2$ . After making the following Fourier expansion of  $\delta\Sigma$  and  $\delta\psi$

$$\begin{aligned} \delta\Sigma(x, y) &= \int d^2k' \delta\Sigma_{\underline{k}'} e^{i\underline{k}' \cdot \underline{x}} \\ \delta\psi(x, y) &= \int d^2k \delta\psi_{\underline{k}} e^{i\underline{k} \cdot \underline{x}} \end{aligned}$$

the second term on the left hand side of (6) can be written

$$\begin{aligned} & \frac{c}{B} \int d^2x \int d^2k' \delta\Sigma_{\underline{k}'} e^{i\underline{k}' \cdot \underline{x}} \hat{z} \times \nabla \left( \int d^2k \delta\psi_{\underline{k}} e^{i\underline{k} \cdot \underline{x}} \right) \cdot \nabla \Sigma_0 \\ &= \frac{c}{B} \iint d^2k d^2k' i \hat{z} \times \underline{k} \cdot \nabla \Sigma_0 \delta\Sigma_{\underline{k}'} \delta\psi_{\underline{k}} \int d^2x e^{i(\underline{k}'+\underline{k}) \cdot \underline{x}} \\ &= \frac{c}{B} \iint d^2k d^2k' i \hat{z} \times \underline{k} \cdot \nabla \Sigma_0 \delta\Sigma_{\underline{k}'} \delta\psi_{\underline{k}} \delta(\underline{k}'+\underline{k}) \\ &= \frac{c}{B} \int d^2k i \hat{z} \times \underline{k} \cdot \nabla \Sigma_0 \delta\Sigma_{-\underline{k}} \delta\psi_{\underline{k}} \end{aligned}$$

where  $\delta(\underline{x})$  is the two-dimensional delta function. The first and fourth terms in equation (6) are reduced in a similar

manner

$$\frac{1}{2} \frac{\partial}{\partial t} \int d^2x (\delta\Sigma)^2 = \frac{1}{2} \frac{\partial}{\partial t} \int d^2k |\delta\Sigma_{\underline{k}}|^2$$

and

$$D \int d^2x \delta\Sigma \nabla^2 \delta\Sigma = - D \int d^2k k^2 |\delta\Sigma_{\underline{k}}|^2$$

All that remains is to find an expression for  $\delta\psi_{\underline{k}}$  to evaluate the second term on the left hand side. Since we are considering only quadratic nonlinearities only a linear relation of  $\delta\psi_{\underline{k}}$  to  $\delta\Sigma_{\underline{k}}$  is needed and one can use the linearized version of equation (5) to find  $\delta\psi_{\underline{k}}$  in terms of  $\delta\Sigma_{\underline{k}}$ .

$$\Sigma_0 \nabla^2 \delta\psi + \nabla \Sigma_0 \cdot \nabla \delta\psi = \underline{E}_0 \cdot \nabla \delta\Sigma \quad (5a)$$

Inserting Fourier expansions of  $\delta\Sigma$  and  $\delta\psi$  into (5a) we find in a straightforward manner

$$\delta\psi_{\underline{k}} \cong - (i \underline{k} \cdot \underline{E}_0 / k^2 \Sigma_0) \delta\Sigma_{\underline{k}} \quad (7)$$

Substituting into the Fourier transformed version of the second term on the left hand side of equation (6) gives

$$\frac{c}{B} \int d^2k (\hat{z} \times \underline{k} \cdot \nabla \Sigma_0 \underline{k} \cdot \underline{E}_0 / k^2 \Sigma_0) |\delta\Sigma_{\underline{k}}|^2$$

Equation (6) can then be written as

$$\frac{1}{2} \frac{\partial}{\partial t} \int d^2k P_{\underline{k}} = \int d^2k \gamma_{\underline{k}} P_{\underline{k}} \quad (8)$$

where  $P_{\underline{k}} \equiv |\delta\Sigma_{\underline{k}}|^2 = |\delta\Sigma(k_x, k_y)|^2$  and  $\gamma_{\underline{k}}$  is the linear growth rate given by

$$\begin{aligned}\gamma_{\underline{k}} &= \frac{c}{B} (\underline{k} \cdot \underline{E}_0 \hat{z} \times \underline{k} \cdot \nabla \Sigma_0 / k^2 \Sigma_0) - Dk^2 \\ &= (cE_0/BL) \cos^2 \theta - Dk^2\end{aligned}$$

where  $L^{-1} = (1/\Sigma_0)(\partial \Sigma_0 / \partial x)$  and  $\theta$  is the angle defined by  $\underline{k}$  and  $\underline{E}_0$ . We note that the nonlinear term does not enter into (8); the nonlinear term thus conserves energy and may be thought of as a bridge between the stable and unstable regions of wave-number space. This property is also shared by several other nonlinear plasma physics problems, e.g., the two-dimensional electrostatic guiding center plasma [Montgomery, 1976], ion-acoustic shock formation [Ott et al., 1973], and two-dimensional turbulence in the equatorial electrojet [Keskinen et al., 1979; Sudan and Keskinen, 1977, 1979].

In the steady state ( $\partial/\partial t = 0$ ) we can write (8) in polar coordinates ( $k^2 = k_x^2 + k_y^2$ ,  $\tan \theta = k_x/k_y$ ) assuming the spatial power spectrum extends from  $k_{\min}$  to  $k_{\max}$

$$\int_{k_{\min}}^{k_c} dk k \int_0^{2\pi} d\theta \gamma_{\underline{k}}^g P_{\underline{k}} = \int_{k_c}^{k_{\max}} dk k \int_0^{2\pi} d\theta \gamma_{\underline{k}}^d P_{\underline{k}} \quad (9)$$

with  $\gamma_{\underline{k}}^g = (cE_0/BL) \cos^2 \theta$  and  $\gamma_{\underline{k}}^d = Dk^2$ . As a result the total power generated in the unstable range of wavenumbers between  $k_{\min}$  and  $k_c$ , the critical wavenumber, must be balanced by the power dissipated in the stable regime between  $k_c$  and  $k_{\max}$  under steady state conditions.

Our approach will be to make an ansatz for  $P(k, \theta)$  and show its consistency with (9). Previous numerical simulation studies

[Scannapieco et al., 1976; Keskinen et al., 1980a; Keskinen and Ossakow, 1980] have shown that the one-dimensional transverse integrated spatial power spectra of magnetic field line integrated Pedersen conductivity perturbations in the plane perpendicular to the magnetic field of initially slablike ionospheric plasma clouds can be represented by a power law, i.e.,

$$\int dk_x |\delta \Sigma(k_x, k_y)|^2 \propto (k_y^2 + k_{oy}^2)^{-n_y/2}$$

and

$$\int dk_y |\delta \Sigma(k_x, k_y)|^2 \propto (k_x^2 + k_{ox}^2)^{-n_x/2}$$

with  $n_x \approx 2$ ,  $n_y \approx 2-3$ , and  $2\pi/k_o$  the outer scale size where the x-axis denotes the direction of plasma cloud  $\underline{E} \times \underline{B}$  drift. These power spectral indices are in agreement with those derived from experimental observations [Baker and Ulwick, 1978; Kelley et al., 1979] of ionospheric plasma clouds. Recently, the angular dependence of  $P(k, \theta)$  has been studied [Keskinen and Ossakow, 1980] in the nonlinear steady state regime for initially slablike ionospheric plasma clouds under different sets of initial conditions. In polar coordinates, these studies show that  $P(k, \theta)$  is anisotropic with maximum power along and near the y-direction (perpendicular to  $\underline{E}_o \times \underline{B}$  direction) and suggest that

$$P(k, \theta) \approx P_o \cos^m \theta (1 + (k/k_o)^2)^{-(n+1)/2}$$

with  $m > 0$ ,  $P_o = \text{const}$ , and  $2\pi/k_o$  is the outer scale size. We note that this form for  $P(k, \theta)$  maximizes in the linearly most unstable direction ( $\theta = 0$  where  $\theta$  is defined by  $\underline{k}$  and  $\underline{E}_o$ ). This anisotropy is a reflection of the fact that nonlinear plasma

cloud striations are elongated much more in the  $\underline{E}_0 \times \underline{B}$  direction and this result is also observed in local simulations of ionospheric plasma clouds [Keskinen et al., 1980b]. The anisotropic nature of the two-dimensional spatial power spectra of ionospheric plasma clouds is also consistent with arguments put forth by Chaturvedi and Ossakow [1979] in discussing the nonlinear stabilization of the  $\underline{E} \times \underline{B}$  gradient-drift instability in ionospheric plasma clouds. In addition, this anisotropy is also observed in experimental plasma cloud studies [M.C. Kelley, private communication, 1980].

We substitute this ansatz for  $P(k, \theta)$  into the left hand side of (9) obtaining

$$\begin{aligned} & (P_0 c E_0 / BL) \int_0^{2\pi} d\theta \cos^{m+2} \theta \int_{k_{\min}}^{k_c} dk k (1 + (k/k_0)^2)^{-(n+1)/2} \\ &= (P_0 c E_0 / BL) 2\sqrt{\pi} \frac{\Gamma(\frac{m+3}{2})}{\Gamma(\frac{m}{2}+2)} \frac{k_0^2}{1-n} \left[ \left(1 + \left(\frac{k_c}{k_0}\right)^2\right)^{(1-n)/2} - \left(1 + \left(\frac{k_{\min}}{k_0}\right)^2\right)^{(1-n)/2} \right] \\ &\approx (P_0 c E_0 / BL) 2\sqrt{\pi} \frac{\Gamma(\frac{m+3}{2})}{\Gamma(\frac{m}{2}+2)} \frac{k_0^2}{n-1} \end{aligned}$$

where  $\Gamma(p)$  is the Gamma-function defined by

$$\Gamma(p) = \int_0^{\infty} dx x^{p-1} e^{-x}$$

and we have assumed  $k_c > k_0$ ,  $k_{\min} < k_0 < k_c$  and  $n > 1$ . Similarly the right hand side of (9) gives

$$P_o D \approx 2\sqrt{\pi} \frac{\Gamma(\frac{m+1}{2})}{\Gamma(\frac{m}{2}+1)} \frac{k_o^4}{3-n} \left(\frac{k_{\max}}{k_o}\right)^{3-n}$$

We note that since the left and right hand sides of (9) must be positive, the spectral index  $k < n < 3$ . This implies that the steady state spatial power spectrum can be represented by a power law. Equating the power generated in the unstable region to the power dissipated and solving for the outer scale wavenumber  $k_o$  we find

$$\left(\frac{k_o}{k_{\max}}\right)^{n-1} = \frac{3-n}{n-1} \frac{\Gamma(\frac{m+1}{2})}{\Gamma(\frac{m}{2}+1)} \frac{\Gamma(\frac{m}{2}+2)}{\Gamma(\frac{m+3}{2})} \frac{(cE_o/BL)}{Dk_{\max}^2} \quad (10)$$

For an inverse power law with spectral index  $n = 2$  and a  $\cos^2\theta$  angular ( $m = 2$ ) dependence we find  $k_o \propto L^{-1}$ . This scaling of outer scale wavenumber  $k_o$  with the initial Pedersen conductivity gradient scale length when  $n \approx 2-3$  is consistent with recent numerical simulation studies of the  $\underline{E} \times \underline{B}$  gradient drift instability in ionospheric plasma clouds [Keskinen et al., 1980a; Keskinen and Ossakow, 1980]. Furthermore, by taking  $D = 1 \text{ m}^2/\text{sec}$ ,  $L = 6 \text{ km}$ ,  $V_o = cE_o/B = 100 \text{ m/sec}$ ,  $2\pi/k_{\max} = 20 \text{ m}$  [McDonald et al., 1978; Baker and Ulwick, 1978] we find from (10) that  $2\pi/k_o \approx 200 \text{ m}$ .

We further note that these results may also be applicable to the natural ionosphere since if one replaces the terms  $D\nabla^2\delta\Sigma$  and  $\underline{E}_o \cdot \nabla\delta\Sigma$  in (4) and (5) with  $-v_R\delta\Sigma$  and  $(\underline{g} \times \underline{z}/v_{in}) \cdot \nabla\delta\Sigma$ ,

respectively, where  $\nu_R$  is a recombination rate,  $g$  denotes gravity, and  $\nu_{in}$  the collision frequency with neutrals, then (4) and (5) are similar to the equations that describe the collisional Rayleigh-Taylor instability [Ossakow et al., 1979] in the equatorial F layer. The adaptation of this method to the collisional Rayleigh-Taylor instability and current convective instability is now in progress.

#### Acknowledgments

This work was supported by the Defense Nuclear Agency.

## References

- Baker, K.D., and J.C. Ulwick, Measurements of Electron Density Structure in Barium Clouds, Geophys. Res. Lett., 5, 723, 1978.
- Chaturvedi, P.K., and S.L. Ossakow, Nonlinear Stabilization of the  $E \times B$  Gradient Drift Instability in Ionospheric Plasma Clouds, J. Geophys. Res., 84, 419, 1979.
- Davis, T.N., G.J. Romick, E.M. Westcott, R.A. Jeffries, D.M. Kerr, and H.M. Peek, Observations of the Development of Striations in Large Barium Clouds, Planet. Space Sci., 22, 67, 1974.
- Doles, J.J., III, N.J. Zabusky, and F.W. Perkins, Deformation and Striation of Plasma Clouds in the Ionosphere, 3, Numerical Simulations of a Multilevel Model with Recombination Chemistry, J. Geophys. Res., 81, 5987, 1976.
- Dungey, J., Cosmic Electrodynamics, Cambridge University Press, London, 1958.
- Goldman, S.R., S.L. Ossakow, and D.L. Book, On the Nonlinear Motion of a small Barium Cloud in the Ionosphere, J. Geophys. Res., 79, 1471, 1974.
- Haerendel, G., R. Lust, and E. Rieger, Motion of Artificial Ion Clouds in the Upper Atmosphere, Planet. Space Sci., 15, 1, 1967.
- Kelley, M.C., K.D. Baker, and J.C. Ulwick, Late Time Barium Cloud Striations and Their Possible Relationship to Equatorial Spread F, J. Geophys. Res., 84, 1898, 1979.



- Keskinen, M.J., B.E. McDonald, and S.L. Ossakow, Preliminary Numerical Study of the Outer Scale Size of Ionospheric Plasma Cloud Striations, J. Geophys. Res., 85, 2349, 1980a.
- Keskinen, M.J., S.L. Ossakow, and P.K. Chaturvedi, Preliminary Report of Numerical Simulations of Intermediate Wavelength  $\underline{E} \times \underline{B}$  Gradient Drift Instability in Ionospheric Plasma Clouds, J. Geophys. Res., 85, 3485 1980b.
- Keskinen, M.J., and S.L. Ossakow, Effects of Different Initial Conditions on the Evolution of the  $\underline{E} \times \underline{B}$  Gradient Drift Instability in Ionospheric Plasma Clouds, submitted to J. Geophys. Res., 1980.
- Keskinen, M.J., R.N. Sudan, and R.L. Ferch, Temporal and Spatial Power Spectrum Studies of Numerical Simulations of the  $\underline{E} \times \underline{B}$  Gradient Drift Type 2 Irregularities in the Equatorial Electrojet, J. Geophys. Res., 84, 1419, 1979.
- Linson, L.M., and J.B. Workman, Formation of Striations in Ionospheric Plasma Clouds, J. Geophys. Res., 75, 3211, 1970.
- Lloyd, J.H., and G. Haerendel, Numerical Modeling of the Drift and Deformation of Ionospheric Plasma Clouds and of their Interaction with Other Layers of the Ionosphere, J. Geophys. Res., 78, 7389, 1973.
- McDonald, B.E., S.L. Ossakow, S.T. Zalesak, and N.J. Zabusky, Determination of Minimum Scale Sizes in Plasma Cloud Striations, in Effect of the Ionosphere on Space and Terrestrial Systems, edited by J.M. Goodman, U.S. Government Printing Office, Washington, D.C. 1978.

- McDonald, B.E., S.L. Ossakow, S.T. Zalesak, and N.J. Zabusky,  
Scale Sizes and Lifetimes of F Region Striations as  
Determined by the Condition of Marginal Stability,  
submitted to J. Geophys. Res., 1980.
- Montgomery, D., Plasma Kinetic Processes in a Strong d.c. Mag-  
netic Field, Physica, 82C, 111, 1976 (and references  
therein).
- Ossakow, S.L., A.J. Scannapieco, S.R. Goldman, D.L. Book, and  
B.E. McDonald, Theoretical and Numerical Simulation Studies  
of Ionospheric Inhomogeneities Produced by Plasma Clouds,  
in Effect of the Ionosphere on Space Systems and Com-  
munications, edited by J.M. Goodman, U.S. Government  
Printing Office, Washington, D.C., 1975.
- Ossakow, S.L., S.T. Zalesak, and N.J. Zabusky, Recent Results  
on Cleavage, Bifurcation, and Cascade Mechanisms in Iono-  
spheric Plasma Clouds, Memo. Rep. 3579, Nav. Res. Lab.,  
Washington, D.C., Aug., 1977.
- Ossakow, S.L., S.T. Zalesak, B.E. McDonald, and P.K. Chaturvedi,  
Nonlinear Equatorial Spread F: Dependence on Altitude of F  
Peak and Bottomside Background Electron Density Gradient  
Scale Length, J. Geophys. Res., 84, 17, 1979.
- Ott, E., W.M. Manheimer, D.L. Book, and J.P. Boris, Model  
Equations for Mode Coupling Saturation in Unstable Plasma,  
Phys. Fluids, 16, 855, 1973.
- Perkins, F.W., N.J. Zabusky, and J.H. Doles, III, Deformation  
and Striation of Plasma Clouds in the Ionosphere, 1, J.  
Geophys. Res., 78, 697, 1973.

- Rognlien, T.D., and J. Weinstock, Theory of the Nonlinear Spectrum of the Gradient Drift Instability in the Equatorial Electrojet, J. Geophys. Res., 79, 4733, 1974.
- Rosenberg, N.W., Observations of Striation Formation in a Barium Ion Cloud, J. Geophys. Res., 76, 6856, 1971.
- Scannapieco, A.J., S.L. Ossakow, S.R. Goldman, and J.M. Pierre, Plasma Cloud Late Time Striation Spectra, J. Geophys. Res., 81, 6037, 1976.
- Simon, A., Instability of a Partially Ionized Plasma in Crossed Electric and Magnetic Fields, Phys. Fluids, 6, 382, 1963.
- Sudan, R.M., and M.J. Keskinen, Theory of Strongly Turbulent two-dimensional Convection of Low-pressure Plasma, Phys. Rev. Lett., 38, 966, 1977.
- Sudan, R.M., and M.J. Keskinen, Theory of Strongly Turbulent Two-dimensional Convection of Low-pressure Plasma, Phys. Fluids, 22, 2305, 1979.
- Völk, H.J., and G. Haerendel, Striations in Ionospheric Clouds, 1, J. Geophys. Res., 76, 4541, 1971.
- Zabusky, N.J., J.H. Doles, III, and F.W. Perkins, Deformation and Striation of Plasma Clouds in the Ionosphere, 2, Numerical Simulation of a Nonlinear Two-dimensional Model, J. Geophys. Res., 78, 711, 1973.

# DISTRIBUTION LIST

## DEPARTMENT OF DEFENSE

### ASSISTANT SECRETARY OF DEFENSE

COMM, COM, COM & INTELL  
WASHINGTON, D.C. 20301  
OICY ATTN J. BARCOCK  
OICY ATTN M. EPSTEIN

### ASSISTANT TO THE SECRETARY OF DEFENSE

ATOMIC ENERGY  
WASHINGTON, D.C. 20301  
OICY ATTN EXECUTIVE ASSISTANT

### DIRECTOR

COMMAND CONTROL TECHNICAL CENTER  
PENTAGON RM BE 685  
WASHINGTON, D.C. 20301  
OICY ATTN C-650  
OICY ATTN C-312 R. MASON

### DIRECTOR

DEFENSE ADVANCED RSCH PROJ AGENCY  
ARCHITECT BUILDING  
1400 WILSON BLVD.  
ARLINGTON, VA. 22209  
OICY ATTN NUCLEAR MONITORING RESEARCH  
OICY ATTN STRATEGIC TECH OFFICE

### DEFENSE COMMUNICATION ENGINEER CENTER

1860 WISNLE AVENUE  
RESTON, VA. 22090  
OICY ATTN CODE R820  
OICY ATTN CODE R410 JAMES W. MCLEAN  
OICY ATTN CODE R720 J. WORTHINGTON

### DIRECTOR

DEFENSE COMMUNICATIONS AGENCY  
WASHINGTON, D.C. 20305  
(ADR CNM01: ATTN CODE 240 FOR)  
OICY ATTN CODE 1018

### DEFENSE TECHNICAL INFORMATION CENTER

CAMERON STATION  
ALEXANDRIA, VA. 22314  
(12 COPIES IF OPEN PUBLICATION, OTHERWISE 2 COPIES)  
OICY ATTN TC

### DIRECTOR

DEFENSE INTELLIGENCE AGENCY  
WASHINGTON, D.C. 20301  
OICY ATTN DT-19  
OICY ATTN DB-4C E. O'FARRELL  
OICY ATTN DIAAP A. WISE  
OICY ATTN DIAST-5  
OICY ATTN DT-182 R. MORTON  
OICY ATTN HQ-TR J. STEWART  
OICY ATTN W. WITTIG OC-7D

### DIRECTOR

DEFENSE NUCLEAR AGENCY  
WASHINGTON, D.C. 20305  
OICY ATTN STVL  
OICY ATTN TITL  
OICY ATTN DOST  
OICY ATTN RAAE

### COMMANDER

FIELD COMMAND  
DEFENSE NUCLEAR AGENCY  
KIRTLAND AFB, NM 87115  
OICY ATTN PCPR

### DIRECTOR

INTERSERVICE NUCLEAR WEAPONS SCHOOL  
KIRTLAND AFB, NM 87115  
OICY ATTN DOCUMENT CONTROL

## JOINT CHIEFS OF STAFF

WASHINGTON, D.C. 20301  
OICY ATTN J-3 NMCCS EVALUATION OFFICE

### DIRECTOR

JOINT STRAT TGT PLANNING STAFF  
OFFUTT AFB  
OMAHA, NB 68113  
OICY ATTN JLTW-2  
OICY ATTN JPST G. GOETZ

### CHIEF

LIVERMORE DIVISION FLD COMMAND DNA  
DEPARTMENT OF DEFENSE  
LAWRENCE LIVERMORE LABORATORY  
P. O. BOX 808  
LIVERMORE, CA 94550  
OICY ATTN PCPRL

### DIRECTOR

NATIONAL SECURITY AGENCY  
DEPARTMENT OF DEFENSE  
FT. GEORGE G. MEADE, MD 20755  
OICY ATTN JOHN SKILLMAN R52  
OICY ATTN FRANK LEONARD  
OICY ATTN W14 PAT CLARK  
OICY ATTN OLIVER M. BARTLETT #32  
OICY ATTN R5

### COMMANDANT

NATO SCHOOL (SHAPE)  
APO NEW YORK 09172  
OICY ATTN U.S. DOCUMENTS OFFICER

### UNDER SECY OF DEF FOR RSCH & ENGRG

DEPARTMENT OF DEFENSE  
WASHINGTON, D.C. 20301  
OICY ATTN STRATEGIC & SPACE SYSTEMS (OS)

### WMCCS SYSTEM ENGINEERING ORG

WASHINGTON, D.C. 20305  
OICY ATTN R. CRAWFORD

### COMMANDER/DIRECTOR

ATMOSPHERIC SCIENCES LABORATORY  
U.S. ARMY ELECTRONICS COMMAND  
WHITE SANDS MISSILE RANGE, NM 88002  
OICY ATTN DELAS-EO F. NILES

### DIRECTOR

BMD ADVANCED TECH CTR  
HUNTSVILLE OFFICE  
P. O. BOX 1500  
HUNTSVILLE, AL 35807  
OICY ATTN ATC-T MELVIN T. CAMPS  
OICY ATTN ATC-O W. DAVIES  
OICY ATTN ATC-R DON RUSS

### PROGRAM MANAGER

BMD PROGRAM OFFICE  
5001 EISENHOWER AVENUE  
ALEXANDRIA, VA 22333  
OICY ATTN DACS-BMT J. SHEA

### CHIEF C-E SERVICES DIVISION

U.S. ARMY COMMUNICATIONS CMD  
PENTAGON RM 1B269  
WASHINGTON, D.C. 20310  
OICY ATTN C-E-SERVICES DIVISION

### COMMANDER

FRACOM TECHNICAL SUPPORT ACTIVITY  
DEPARTMENT OF THE ARMY  
FORT MONMOUTH, N.J. 07703  
OICY ATTN DRSEL-AL-RO M. BENNET  
OICY ATTN DRSEL-PL-ENV M. BONKE  
OICY ATTN J. E. QUIGLEY

COMMANDER  
HARRY DIAMOND LABORATORIES  
DEPARTMENT OF THE ARMY  
2800 POWDER MILL ROAD  
ADELPHI, MD 20783  
(CNMCI-INNER ENVELOPE: ATTN: DELHO-RBH)  
O1CY ATTN DELHO-TI M. WEINER  
O1CY ATTN DELHO-RB R. WILLIAMS  
O1CY ATTN DELHO-NP P. WIMENITZ  
O1CY ATTN DELHO-NP C. MOAZED

COMMANDER  
U.S. ARMY COMM-ELEC ENGRG INSTAL AGY  
FT. HUACHUCA, AZ 85613  
O1CY ATTN CCC-EHEO GEORGE LANE

COMMANDER  
U.S. ARMY FOREIGN SCIENCE & TECH CTR  
220 7TH STREET, NE  
CHARLOTTESVILLE, VA 22901  
O1CY ATTN DRXST-SD  
O1CY ATTN R. JONES

COMMANDER  
U.S. ARMY MATERIEL DEV & READINESS CMD  
5001 EISENHOWER AVENUE  
ALEXANDRIA, VA 22333  
O1CY ATTN DRCLDC J. A. BENDER

COMMANDER  
U.S. ARMY NUCLEAR AND CHEMICAL AGENCY  
7500 BACKLICK ROAD  
BLOG 2073  
SPRINGFIELD, VA 22150  
O1CY ATTN LIBRARY

DIRECTOR  
U.S. ARMY BALLISTIC RESEARCH LABS  
ABERDEEN PROVING GROUND, MD 21005  
O1CY ATTN TECH LIB EDWARD BAICY

COMMANDER  
U.S. ARMY SATCOM AGENCY  
FT. MONMOUTH, NJ 07703  
O1CY ATTN DOCUMENT CONTROL

COMMANDER  
J.S. ARMY MISSILE INTELLIGENCE AGENCY  
REDSTONE ARSENAL, AL 35809  
O1CY ATTN JIM GAMBLE

DIRECTOR  
U.S. ARMY TRADOC SYSTEMS ANALYSIS ACTIVITY  
WHITE SANDS MISSILE RANGE, NM 88002  
O1CY ATTN ATAA-SA  
O1CY ATTN TCC/F. PAYAN JR.  
O1CY ATTN ATAA-TAC LTC J. HESSE

COMMANDER  
NAVAL ELECTRONIC SYSTEMS COMMAND  
WASHINGTON, D.C. 20360  
O1CY ATTN NAVALEX 034 T. HUGHES  
O1CY ATTN PNE 117  
O1CY ATTN PNE 117-T  
O1CY ATTN CODE 5011

COMMANDING OFFICER  
NAVAL INTELLIGENCE SUPPORT CTR  
4301 SUITLAND ROAD, BLDG. 5  
WASHINGTON, D.C. 20390  
O1CY ATTN MR. DUBBIN STIC 12  
O1CY ATTN NISC-50  
O1CY ATTN CODE 5404 J. GALET

COMMANDER  
NAVAL OCEAN SYSTEMS CENTER  
SAN DIEGO, CA 92152  
O1CY ATTN CODE 532 W. MOLER  
O1CY ATTN CODE 0230 C. BAGGETT  
O1CY ATTN CODE 81 R. EASTMAN

DIRECTOR  
NAVAL RESEARCH LABORATORY  
WASHINGTON, D.C. 20375  
O1CY ATTN CODE 4700 T. P. COFFEY (25 CYS IF UN, 1 CY IF CLASS)  
O1CY ATTN CODE 4701 JACK D. BROWN  
O1CY ATTN CODE 4780 BRANCH HEAD (150 CYS IF UN, 1 CY IF CLASS)  
O1CY ATTN CODE 7500 HQ COMM DIR BRUCE WALD  
O1CY ATTN CODE 7550 J. DAVIS  
O1CY ATTN CODE 7580  
O1CY ATTN CODE 7551  
O1CY ATTN CODE 7555  
O1CY ATTN CODE 4730 E. MCLEAN

COMMANDER  
NAVAL SEA SYSTEMS COMMAND  
WASHINGTON, D.C. 20362  
O1CY ATTN CAPT R. PITKIN

COMMANDER  
NAVAL SPACE SURVEILLANCE SYSTEM  
DAHLGREN, VA 22448  
O1CY ATTN CAPT J. H. BURTON

OFFICER-IN-CHARGE  
NAVAL SURFACE WEAPONS CENTER  
WHITE OAK, SILVER SPRING, MD 20910  
O1CY ATTN CODE F31

DIRECTOR  
STRATEGIC SYSTEMS PROJECT OFFICE  
DEPARTMENT OF THE NAVY  
WASHINGTON, D.C. 20376  
O1CY ATTN NSP-2141  
O1CY ATTN NSSP-2722 FRED WIMBERLY

NAVAL SPACE SYSTEM ACTIVITY  
P. O. BOX 92960  
WORLDWAY POSTAL CENTER  
LOS ANGELES, CALIF. 90009  
O1CY ATTN A. B. HAZZARD

COMMANDER  
NAVAL SURFACE WEAPONS CENTER  
DAHLGREN LABORATORY  
DAHLGREN, VA 22448  
O1CY ATTN CODE DF-14 R. BUTLER

COMMANDING OFFICER  
NAVY SPACE SYSTEMS ACTIVITY  
P.O. BOX 92960  
WORLDWAY POSTAL CENTER  
LOS ANGELES, CA. 90009  
O1CY ATTN CODE 52

OFFICE OF NAVAL RESEARCH  
ARLINGTON, VA 22217  
O1CY ATTN CODE 465  
O1CY ATTN CODE 461  
O1CY ATTN CODE 402  
O1CY ATTN CODE 420  
O1CY ATTN CODE 421

COMMANDER  
AEROSPACE DEFENSE COMMAND/DC  
DEPARTMENT OF THE AIR FORCE  
ENT AFB, CO 80912  
O1CY ATTN DC MR. LONG

COMMANDER  
AEROSPACE DEFENSE COMMAND/XPD  
DEPARTMENT OF THE AIR FORCE  
ENT AFB, CO 80912  
O1CY ATTN XPDQ  
O1CY ATTN XP

AIR FORCE GEOPHYSICS LABORATORY  
HANSCOM AFB, MA 01731  
O1CY ATTN OPR HAROLD GARDNER  
O1CY ATTN OPR-1 JAMES C. ULWICK  
O1CY ATTN LKB KENNETH S. W. CHAMPION  
O1CY ATTN OPR ALVA T. STAIR  
O1CY ATTN PMP JULES AARONS  
O1CY ATTN PHD JURGEN BUCHAU  
O1CY ATTN PHD JOHN P. MULLEN

AF WEAPONS LABORATORY  
KIRTLAND AFB, NM 87117

OICY ATTN SUL  
OICY ATTN CA ARTHUR H. GUENTHER  
OICY ATTN DYC CAPT J. BARRY  
OICY ATTN DYC JOHN M. KAMM  
OICY ATTN DYT CAPT MARK A. FRY  
OICY ATTN DES MAJ GARY GANDONG  
OICY ATTN DYC J. JANNI

AFTAC

PATRICK AFB, FL 32925  
OICY ATTN TF/MAJ WILEY  
OICY ATTN TN

AIR FORCE Wright Aeronautical Laboratories

WRIGHT-PATTERSON AFB, OH 45433  
OICY ATTN AAD WADE HUNT  
OICY ATTN AAD ALLEN JOHNSON

DEPUTY CHIEF OF STAFF

RESEARCH, DEVELOPMENT, & ACQ  
DEPARTMENT OF THE AIR FORCE  
WASHINGTON, D.C. 20330  
OICY ATTN AFRDQ

HEADQUARTERS

ELECTRONIC SYSTEMS DIVISION/XR  
DEPARTMENT OF THE AIR FORCE  
HANSCOM AFB, MA 01731  
OICY ATTN XR J. DEAS

HEADQUARTERS

ELECTRONIC SYSTEMS DIVISION/YSEA  
DEPARTMENT OF THE AIR FORCE  
HANSCOM AFB, MA 01731  
OICY ATTN YSEA

HEADQUARTERS

ELECTRONIC SYSTEMS DIVISION/DC  
DEPARTMENT OF THE AIR FORCE  
HANSCOM AFB, MA 01731  
OICY ATTN DCKC MAJ J.C. CLARK

COMMANDER

FOREIGN TECHNOLOGY DIVISION, AFSC  
WRIGHT-PATTERSON AFB, OH 45433  
OICY ATTN NICO LIBRARY  
OICY ATTN ETOP S. BALLARD

COMMANDER

ROME AIR DEVELOPMENT CENTER, AFSC  
GRIFFISS AFB, NY 13441  
OICY ATTN DOC LIBRARY/TSLO  
OICY ATTN DCSE V. COYNE

SAMSO/SZ

POST OFFICE BOX 92960  
WORLDWAY POSTAL CENTER  
LOS ANGELES, CA 90009  
(SPACE DEFENSE SYSTEMS)  
OICY ATTN SZU

STRATEGIC AIR COMMAND/XPFS

OFFUTT AFB, NE 68113  
OICY ATTN XPFS MAJ B. STEPHAN  
OICY ATTN ADWATE MAJ BRUCE BAUER  
OICY ATTN NRT  
OICY ATTN DOK CHIEF SCIENTIST

SAMSO/SK

P. O. BOX 92960  
WORLDWAY POSTAL CENTER  
LOS ANGELES, CA 90009  
OICY ATTN SKA (SPACE COMM SYSTEMS) M. CLAVIN

SAMSO/MN

NORTON AFB, CA 92409  
(MINUTEMAN)  
OICY ATTN MNAL LTC KENNEDY

COMMANDER

ROME AIR DEVELOPMENT CENTER, AFSC  
HANSCOM AFB, MA 01731  
OICY ATTN EEP A. LORENTZEN

DEPARTMENT OF ENERGY

ALBUQUERQUE OPERATIONS OFFICE  
P. O. BOX 5400  
ALBUQUERQUE, NM 87115  
OICY ATTN DOC CON FOR D. SHERWOOD

DEPARTMENT OF ENERGY

LIBRARY ROOM G-042  
WASHINGTON, D.C. 20545  
OICY ATTN DOC CON FOR A. LABOWITZ

EG&G, INC.

LOS ALAMOS DIVISION  
P. O. BOX 809  
LOS ALAMOS, NM 85544  
OICY ATTN DOC CON FOR J. BREEDLOVE

UNIVERSITY OF CALIFORNIA

LAWRENCE LIVERMORE LABORATORY  
P. O. BOX 808  
LIVERMORE, CA 94550  
OICY ATTN DOC CON FOR TECH INFO DEPT  
OICY ATTN DOC CON FOR L-389 R. OTT  
OICY ATTN DOC CON FOR L-31 R. MAGER  
OICY ATTN DOC CON FOR L-46 F. SEWARD

LOS ALAMOS SCIENTIFIC LABORATORY

P. O. BOX 1663  
LOS ALAMOS, NM 87545  
OICY ATTN DOC CON FOR J. WOLCOTT  
OICY ATTN DOC CON FOR R. F. TASCHER  
OICY ATTN DOC CON FOR E. JONES  
OICY ATTN DOC CON FOR J. MALIK  
OICY ATTN DOC CON FOR R. JEFFRIES  
OICY ATTN DOC CON FOR J. ZINN  
OICY ATTN DOC CON FOR P. KEATON  
OICY ATTN DOC CON FOR D. WESTERVELT

SANDIA LABORATORIES

P. O. BOX 5800  
ALBUQUERQUE, NM 87115  
OICY ATTN DOC CON FOR J. MARTIN  
OICY ATTN DOC CON FOR W. BROWN  
OICY ATTN DOC CON FOR A. THORNBROUGH  
OICY ATTN DOC CON FOR T. WRIGHT  
OICY ATTN DOC CON FOR D. DAHLGREN  
OICY ATTN DOC CON FOR 3141  
OICY ATTN DOC CON FOR SPACE PROJECT DIV

SANDIA LABORATORIES

LIVERMORE LABORATORY  
P. O. BOX 969  
LIVERMORE, CA 94550  
OICY ATTN DOC CON FOR B. MURPHY  
OICY ATTN DOC CON FOR T. COOK

OFFICE OF MILITARY APPLICATION

DEPARTMENT OF ENERGY  
WASHINGTON, D.C. 20545  
OICY ATTN DOC CON FOR D. GALE

OTHER GOVERNMENT

CENTRAL INTELLIGENCE AGENCY

ATTN RD/SI, RM 5G48, HQ BLDG  
WASHINGTON, D.C. 20505  
OICY ATTN OSI/PSID RM 5F 19

DEPARTMENT OF COMMERCE

NATIONAL BUREAU OF STANDARDS  
WASHINGTON, D.C. 20234  
(ALL CORRES: ATTN SEC OFFICER FOR)  
OICY ATTN R. MOORE

INSTITUTE FOR TELECOM SCIENCES  
NATIONAL TELECOMMUNICATIONS & INFO ADMIN  
BOULDER, CO 80303

OICY ATTN A. JEAN (UNCLASS ONLY)  
OICY ATTN W. U'LAU  
OICY ATTN D. CROMBIE  
OICY ATTN L. BERRY

NATIONAL OCEANIC & ATMOSPHERIC ADMIN  
ENVIRONMENTAL RESEARCH LABORATORIES  
DEPARTMENT OF COMMERCE  
BOULDER, CO 80302

OICY ATTN R. GRUBB  
OICY ATTN AERONOMY LAB G. REID

DEPARTMENT OF DEFENSE CONTRACTORS

AEROSPACE CORPORATION

P. O. BOX 92957

LOS ANGELES, CA 90009

OICY ATTN I. GARPUNKEL  
OICY ATTN T. SALMI  
OICY ATTN V. JOSEPHSON  
OICY ATTN S. BOWER  
OICY ATTN N. STOCKWELL  
OICY ATTN D. OLSEN

OICY ATTN SHFA FOR PMW

ANALYTICAL SYSTEMS ENGINEERING CORP

5 OLD CONCORD ROAD

BURLINGTON, MA 01803

OICY ATTN RADIO SCIENCES

BERKELEY RESEARCH ASSOCIATES, INC.

P. O. BOX 983

BERKELEY, CA 94701

OICY ATTN J. WORKMAN

BOEING COMPANY, THE

P. O. BOX 3707

SEATTLE, WA 98124

OICY ATTN G. KEISTER  
OICY ATTN D. MURRAY  
OICY ATTN G. HALL  
OICY ATTN J. KENNEY

CALIFORNIA AT SAN DIEGO, UNIV OF

P.O. Box 6049

San Diego, CA 92106

BROWN ENGINEERING COMPANY, INC.

CUMMINGS RESEARCH PARK

MUNTSVILLE, AL 35807

OICY ATTN ROMEO A. DELIBERIS

CHARLES STARK DRAPER LABORATORY, INC.

555 TECHNOLOGY SQUARE

CAMBRIDGE, MA 02139

OICY ATTN D. B. COX  
OICY ATTN J. P. GILMORE

COMSAT LABORATORIES

LINTHICUM ROAD

CLARKSBURG, MD 20734

OICY ATTN G. HYDE

CORNELL UNIVERSITY

DEPARTMENT OF ELECTRICAL ENGINEERING

ITHACA, NY 14850

OICY ATTN J. T. FARLEY JR

ELECTROSPACE SYSTEMS, INC.

BOX 1359

RICHARDSON, TX 75080

OICY ATTN M. LOGSTON

OICY ATTN SECURITY (PAUL PHILLIPS)

ESL INC.

495 JAVA DRIVE

SUNNYVALE, CA 94086

OICY ATTN J. ROBERTS

OICY ATTN JAMES MARSHALL

OICY ATTN C. W. PRETTIE

FORD AEROSPACE & COMMUNICATIONS CORP

3939 FABIAN WAY

PALO ALTO, CA 94303

OICY ATTN J. T. MATTINGLEY

GENERAL ELECTRIC COMPANY

SPACE DIVISION

VALLEY FORGE SPACE CENTER

GODDARD BLVD KING OF PRUSSIA

P. O. BOX 8555

PHILADELPHIA, PA 19101

OICY ATTN M. M. BORTNER SPACE SCI LAB

GENERAL ELECTRIC COMPANY

P. O. BOX 1122

SYRACUSE, NY 13201

OICY ATTN F. REIBERT

GENERAL ELECTRIC COMPANY

TEMPO-CENTER FOR ADVANCED STUDIES

816 STATE STREET (P.O. DRAWER QQ)

SANTA BARBARA, CA 93102

OICY ATTN DASTAC

OICY ATTN DON CHANDLER

OICY ATTN TOM BARRETT

OICY ATTN TIM STEPHANS

OICY ATTN WARREN S. KNAPP

OICY ATTN WILLIAM MCNAMARA

OICY ATTN B. GAMBILL

OICY ATTN MACK STANTON

GENERAL ELECTRIC TECH SERVICES CO., INC.

HMES

COURT STREET

SYRACUSE, NY 13201

OICY ATTN G. MILLMAN

GENERAL RESEARCH CORPORATION

SANTA BARBARA DIVISION

P. O. BOX 6770

SANTA BARBARA, CA 93111

OICY ATTN JOHN ISE JR

OICY ATTN JOEL GARBARINO

GEOPHYSICAL INSTITUTE

UNIVERSITY OF ALASKA

FAIRBANKS, AK 99701

(ALL CLASS ATTN: SECURITY OFFICER)

OICY ATTN T. N. DAVIS (UNCL ONLY)

OICY ATTN NEAL BROWN (UNCL ONLY)

OICY ATTN TECHNICAL LIBRARY

GTE SYLVANIA, INC.

ELECTRONICS SYSTEMS GRP-EASTERN DIV

77 A STREET

NEEDHAM, MA 02194

OICY ATTN MARSHAL CROSS

ILLINOIS, UNIVERSITY OF

DEPARTMENT OF ELECTRICAL ENGINEERING

URBANA, IL 61803

OICY ATTN K. YEH

ILLINOIS, UNIVERSITY OF

107 COBLE HALL

801 S. WRIGHT STREET

URBANA, IL 60680

(ALL CORRES ATTN SECURITY SUPERVISOR FOR)

OICY ATTN K. YEH

INSTITUTE FOR DEFENSE ANALYSES  
400 ARMY-NAVY DRIVE  
ARLINGTON, VA 22202  
OICY ATTN J. M. AEIN  
OICY ATTN ERNEST BAUER  
OICY ATTN HANS WOLFHARD  
OICY ATTN JOEL BENGSTON

HSS, INC.  
2 ALFRED CIRCLE  
BEDFORD, MA 01730  
OICY ATTN DONALD HANSEN

INTL TEL & TELEGRAPH CORPORATION  
500 WASHINGTON AVENUE  
NUTLEY, NJ 07110  
OICY ATTN TECHNICAL LIBRARY

JAYCOR  
1401 CAMINO DEL MAR  
DEL MAR, CA 32014  
OICY ATTN S. R. GOLDMAN

JOHNS HOPKINS UNIVERSITY  
APPLIED PHYSICS LABORATORY  
JOHNS HOPKINS ROAD  
LAUREL, MD 20810  
OICY ATTN DOCUMENT LIBRARIAN  
OICY ATTN THOMAS POTEMRA  
OICY ATTN JOHN DASSOULAS

LOCKHEED MISSILES & SPACE CO INC  
P. O. BOX 504  
SUNNYVALE, CA 94088  
OICY ATTN DEPT 60-12  
OICY ATTN D. R. CHURCHILL

LOCKHEED MISSILES AND SPACE CO INC  
3251 HANOVER STREET  
PALO ALTO, CA 94304  
OICY ATTN MARTIN WALT DEPT 52-10  
OICY ATTN RICHARD G. JOHNSON DEPT 52-12  
OICY ATTN W. L. IMHOFF DEPT 52-12

KAMAN SCIENCES CORP  
P. O. BOX 7463  
COLORADO SPRINGS, CO 80933  
OICY ATTN T. MEAGHER

LINKABIT CORP  
10453 ROSELLE  
SAN DIEGO, CA 92121  
OICY ATTN IRWIN JACOBS

M.I.T. LINCOLN LABORATORY  
P. O. BOX 73  
LEXINGTON, MA 02173  
OICY ATTN DAVID M. TOWLE  
OICY ATTN P. WALDRON  
OICY ATTN L. LOUGHLIN  
OICY ATTN D. CLARK

MARTIN MARIETTA CORP  
ORLANDO DIVISION  
P. O. BOX 5837  
ORLANDO, FL 32805  
OICY ATTN R. HEFFNER

MCDONNELL DOUGLAS CORPORATION  
5301 BOLSA AVENUE  
HUNTINGTON BEACH, CA 92647  
OICY ATTN N. HARRIS  
OICY ATTN J. MOULE  
OICY ATTN GEORGE MROZ  
OICY ATTN W. OLSON  
OICY ATTN R. W. HALPRIN  
OICY ATTN TECHNICAL LIBRARY SERVICES

MISSION RESEARCH CORPORATION  
735 STATE STREET  
SANTA BARBARA, CA 93101  
OICY ATTN P. FISCHER  
OICY ATTN W. F. CREVIER  
OICY ATTN STEVEN L. GUTSCHE  
OICY ATTN D. SAPPENFIELD  
OICY ATTN R. BOGUSCH  
OICY ATTN R. HENDRICK  
OICY ATTN RALPH KILB  
OICY ATTN DAVE SOMLE  
OICY ATTN F. FAJEN  
OICY ATTN M. SCHEIBER  
OICY ATTN CONRAD L. LONGMIRE  
OICY ATTN WARREN A. SCHLUETER

MITRE CORPORATION, THE  
P. O. BOX 208  
BEDFORD, MA 01730  
OICY ATTN JOHN MORGANSTERN  
OICY ATTN G. HARDING  
OICY ATTN C. E. CALLAHAN

MITRE CORP  
WESTGATE RESEARCH PARK  
1820 DOLLY MADISON BLVD  
MCLEAN, VA 22101  
OICY ATTN W. HALL  
OICY ATTN W. FOSTER

PACIFIC-SIERRA RESEARCH CORP  
1456 CLOVERFIELD BLVD.  
SANTA MONICA, CA 90404  
OICY ATTN E. C. FIELD JR

PENNSYLVANIA STATE UNIVERSITY  
IONOSPHERE RESEARCH LAB  
318 ELECTRICAL ENGINEERING EAST  
UNIVERSITY PARK, PA 15802  
(NO CLASSIFIED TO THIS ADDRESS)  
OICY ATTN IONOSPHERIC RESEARCH LAB

PHOTOMETRICS, INC.  
442 MARRETT ROAD  
LEXINGTON, MA 02173  
OICY ATTN IRVING L. KOFSKY

PHYSICAL DYNAMICS INC.  
P. O. BOX 3027  
BELLEVUE, WA 98009  
OICY ATTN E. J. FREMOW

PHYSICAL DYNAMICS INC.  
P. O. BOX 10367  
OAKLAND, CA. 94610  
ATTN: A. THOMSON

R & D ASSOCIATES  
P. O. BOX 9695  
MARINA DEL REY, CA 90291  
OICY ATTN FORREST GILMORE  
OICY ATTN BRYAN GABBARD  
OICY ATTN WILLIAM B. WRIGHT JR  
OICY ATTN ROBERT F. LELEVIER  
OICY ATTN WILLIAM J. KARZAS  
OICY ATTN H. DRY  
OICY ATTN C. MACDONALD  
OICY ATTN R. TURCO

RAND CORPORATION, THE  
1700 MAIN STREET  
SANTA MONICA, CA 90406  
OICY ATTN CULLEN CRAIN  
OICY ATTN ED BEDROZIAN

RIVERSIDE RESEARCH INSTITUTE  
80 WEST END AVENUE  
NEW YORK, NY 10023  
OICY ATTN VINCE TRAPANI



SCIENCE APPLICATIONS, INC.  
P. O. BOX 2351  
LA JOLLA, CA 92038

01CY ATTN LEWIS M. LINSON  
01CY ATTN DANIEL A. HAMLIN  
01CY ATTN D. SACHS  
01CY ATTN E. A. STRAKER  
01CY ATTN CURTIS A. SMITH  
01CY ATTN JACK MCDUGALL

Raytheon Co.  
528 Boston Post Road  
Sudbury, MA 01776  
01CY ATTN Barbara Adams

Science Applications, Incorporated  
1710 Goodridge Dr.  
McLean, VA 22102  
Attn: J. Cockayne

Lockheed Missile & Space Co., Inc.  
Huntsville Research & Engr. Ctr.  
4800 Bradford Drive  
Huntsville, Alabama 35807  
Attn: Dale H. Davis

SRI INTERNATIONAL  
333 RAVENSWOOD AVENUE  
MENLO PARK, CA 94025

01CY ATTN DONALD NEILSON  
01CY ATTN ALAN BURNS  
01CY ATTN G. SMITH  
01CY ATTN L. L. COBB  
01CY ATTN DAVID A. JOHNSON  
01CY ATTN WALTER G. CHESNUT  
01CY ATTN CHARLES L. RIND  
01CY ATTN WALTER JAYE  
01CY ATTN M. BARON  
01CY ATTN RAY L. LEADABRAND  
01CY ATTN G. CARPENTER  
01CY ATTN G. PRICE  
01CY ATTN J. PETERSON  
01CY ATTN R. MAKE, JR.  
01CY ATTN V. GONZALES  
01CY ATTN D. MCDANIEL

TECHNOLOGY INTERNATIONAL CORP  
75 WIGGINS AVENUE  
BEDFORD, MA 01730  
01CY ATTN W. P. BOQUIST

TRW DEFENSE & SPACE SYS GROUP  
ONE SPACE PARK  
REDONDO BEACH, CA 90278  
01CY ATTN R. K. PLEBUCH  
01CY ATTN S. ALTSCHULER  
01CY ATTN D. DEE

VISIDYNE, INC.  
19 THIRD AVENUE  
NORTH WEST INDUSTRIAL PARK  
BURLINGTON, MA 01803  
01CY ATTN CHARLES HUMPHREY  
01CY ATTN J. W. CARPENTER

IONOSPHERIC MODELING DISTRIBUTION LIST  
UNCLASSIFIED ONLY

PLEASE DISTRIBUTE ONE COPY TO EACH OF THE FOLLOWING PEOPLE:

ADVANCED RESEARCH PROJECTS AGENCY (ARPA)  
STRATEGIC TECHNOLOGY OFFICE  
ARLINGTON, VIRGINIA

CAPT. DONALD M. LEVINE

NAVAL RESEARCH LABORATORY  
WASHINGTON, D.C. 20375

DR. P. MANGE  
DR. R. MEIER  
DR. E. SZUSZCZEWICZ - CODE 4127  
DR. TIMOTHY COFFEY - CODE 4700 (25 COPIES)  
DR. S. OSSAKOW - CODE 4780 (100 COPIES)  
DR. J. GOODMAN - CODE 7560

SCIENCE APPLICATIONS, INC.  
1250 PROSPECT PLAZA  
LA JOLLA, CALIFORNIA 92037

DR. D. A. HAMLIN  
DR. L. LINSON  
DR. D. SACHS

DIRECTOR OF SPACE AND ENVIRONMENTAL LABORATORY  
NOAA  
BOULDER, COLORADO 80302

DR. A. GLENN JEAN  
DR. G. W. ADAMS  
DR. D. N. ANDERSON  
DR. K. DAVIES  
DR. R. F. DONNELLY

A. F. GEOPHYSICS LABORATORY  
L. G. HANSON FIELD  
BEDFORD, MASS. 01730

DR. T. ELKINS  
DR. W. SWIDER  
MRS. R. SAGALYN  
DR. J. M. FORBES  
DR. T. J. KENESHEA  
DR. J. AARONS

OFFICE OF NAVAL RESEARCH  
800 NORTH QUINCY STREET  
ARLINGTON, VIRGINIA 22217

DR. H. MULLANEY

COMMANDER  
NAVAL ELECTRONICS LABORATORY CENTER  
SAN DIEGO, CALIFORNIA 92152

DR. M. BLEIWEISS  
DR. I. ROTHMULLER  
DR. V. HILDEBRAND  
MR. R. ROSE

U. S. ARMY ABERDEEN RESEARCH AND DEVELOPMENT CENTER  
BALLISTIC RESEARCH LABORATORY  
ABERDEEN, MARYLAND

DR. J. MEIERL

COMMANDER  
NAVAL AIR SYSTEMS COMMAND  
DEPARTMENT OF THE NAVY  
WASHINGTON, D.C. 20360

DR. T. CZUBA

HARVARD UNIVERSITY  
HARVARD SQUARE  
CAMBRIDGE, MASS. 02138

DR. M. B. MCELROY  
DR. R. LINDZEN

PENNSYLVANIA STATE UNIVERSITY  
UNIVERSITY PARK, PENNSYLVANIA 16802

DR. J. S. NISBET  
DR. P. R. ROHRBAUGH  
DR. D. E. BARAN  
DR. L. A. CARPENTER  
DR. M. LEE  
DR. R. DIVANY  
DR. P. BENNETT  
DR. E. KLEVANS

UNIVERSITY OF CALIFORNIA, LOS ANGELES  
405 HILLGARD AVENUE  
LOS ANGELES, CALIFORNIA 90024

DR. F. V. CORONITI  
DR. C. KENNEL

UNIVERSITY OF CALIFORNIA, BERKELEY  
BERKELEY, CALIFORNIA 94720

DR. M. HUDSON

UTAH STATE UNIVERSITY  
4TH N. AND 8TH STREETS  
LOGAN, UTAH 84322

DR. P. M. BANKS  
DR. R. HARRIS  
DR. V. PETERSON  
DR. R. MEGILL  
DR. K. BAKER

CORNELL UNIVERSITY  
ITHACA, NEW YORK 14850

DR. W. E. SWARTZ  
DR. R. SUDAN  
DR. D. FARLEY  
DR. M. KELLEY

NASA  
GODDARD SPACE FLIGHT CENTER  
GREENBELT, MARYLAND 20771

DR. S. CHANDRA  
DR. K. MAEDO

PRINCETON UNIVERSITY  
PLASMA PHYSICS LABORATORY  
PRINCETON, NEW JERSEY 08540

DR. F. PERKINS  
DR. E. FRIEMAN

INSTITUTE FOR DEFENSE ANALYSIS  
400 ARMY/NAVY DRIVE  
ARLINGTON, VIRGINIA 22202

DR. E. BAUER

UNIVERSITY OF MARYLAND  
COLLEGE PARK, MD 20742  
DR. K. PAPADOPOULOS  
DR. E. OTT

UNIVERSITY OF PITTSBURGH  
PITTSBURGH, PA. 15213

DR. N. ZABUSKY  
DR. M. BIONDI

DEFENSE DOCUMENTATION CENTER  
CAMERON STATION  
ALEXANDRIA, VA. 22314

(12 COPIES IF OPEN PUBLICATION  
OTHERWISE 2 COPIES) 12CY ATTN TC

UNIVERSITY OF CALIFORNIA  
LOS ALAMOS SCIENTIFIC LABORATORY  
J-10, MS-664  
LOS ALAMOS, NEW MEXICO 87545

M. PONGRATZ  
D. SIMONS  
G. BARASCH  
L. DUNCAN

Massachusetts Institute of Technology  
Plasma Fusion Center  
Library, NW16-262  
Cambridge, MA 02139

University of California, San Diego  
Dept. of Electrical Engineering  
& Computer Sciences  
Mail Code C-014  
La Jolla, CA 92093

Dr. Henry G. Booker

DATE  
FILMED  
-8